

Midwinter meeting in discrete probability

January 14-15, 2026, Umeå

All talks are in room MIT.C.413 in the MIT-building.

Each speaker has either a 35 minute time slot followed by five minutes for questions and time for the next speaker to prepare.

Wednesday

9.00 Welcome

9.00-9.35 He Guo: Semi-random greedy independent set algorithm

We study a semi-random (Rodl nibble) variant of the random greedy independent set algorithm to construct a large independent set in a hypergraph. Let $r \geq 2$ be a fixed integer and let \mathcal{H} be a r -uniform N -vertex hypergraph satisfying that each vertex is contained in at most D edges. Assuming $\min\{N^{r-1}/D, D\} \geq f$ for some $f \geq (\log N)^c$ with $c > 0$, we prove that if \mathcal{H} satisfies some degree and codegree conditions, then with high probability there are $\Omega\left(N\left(\frac{\log f}{D}\right)^{\frac{1}{r-1}}\right)$ vertices in the independent set constructed by the algorithm.

A key improvement of this semi-random variant compared to Bennett and Bohman's previous random greedy version is that we replace their requirement of \mathcal{H} being D -regular by the maximum degree condition. We also prove that the independent set constructed by this algorithm has various pseudo-random properties, including those needed for applications in Ramsey theory. And we prove that the same holds for a random subhypergraph, i.e., the above properties remain true in the sparse setting.

Based on joint work with Lutz Warnke.

9.40-10.15 Svante Janson: Simply generated trees conditioned on the number of vertices of given degrees.

It is well known that simply generated trees with a given number of vertices include Galton-Watson trees conditioned on a given number of vertices, and that simply generated trees often, but not always, can be reduced to the Galton-Watson case by tilting. This extends to trees with a given number of leaves, or more generally a given number of vertices with degrees in some given set. The Galton-Watson case has been studied by several authors, including Rizzolo,

Kortchemski, Abraham & Delmas. I will discuss extensions of their results and methods, in particular tilting, to the simply generated setting.

10.20-10.40 Coffee

10.40-11.15 Fredrik Scheie : Sequential acquisition process for finite agents

We here introduce a population model called the sequential acquisition model (SAM), a neutral model of cultural evolution formulated as a time-homogeneous Markov jump process where a finite population of N agents sequentially invent, acquire, and forget traits in continuous time. The aim of this talk will be to discuss properties of the SAM model. We here analyze the resulting trait-repertoire dynamics and show that SAM admits a unique limiting distribution. From this distribution, we can derive explicit expressions for the expected number of traits at equilibrium, which depend among others on a parameter α , describing the rate of the socially transmitted traits through an acquisition process. We further obtain results for the expected number of traits carried per agent and characterize the duration of the accumulation process. Together, these results provide a tractable baseline for studying sequential cultural transmission where we hope future population models may further build upon this work. This is a joint work with Fredrik Jansson and Jonas Sjöstrand.

11.20-11.55 Amin Coja-Oghlan: The Ising model on random graphs at low temperature

We revisit the Ising model on sparse Erdos-Renyi random graphs. While a first order approximation to the free energy density was obtained by Dembo and Montanari (2010), here we aim to identify the precise limiting distribution of this random variable. Specifically, we establish a central limit theorem in the low temperature regime. Along the way we clarify the 'pure states' of the model, a question that had not been answered satisfactorily in prior work.

Lunch 12.00-13.15

13.15-13.50 Pavel Zakharov: The Ising model on random graphs: high temperature behaviour.

The Ising model provides one of the clearest examples of a nontrivial phase transition. Lyons identified the existence of such transition on trees and tree-like graphs. We show that, in the absence of an external magnetic field, the free energy of the Ising model on Erdos-Renyi random graphs superconcentrates, as opposed to the low-temperature regime.

13.55–14.30 Julien Verges: Lower-tail large deviations in first-passage percolation

Endow every edge of the usual Z^2 lattice with a random positive weights, and consider the associated random metric T . It is known that almost surely, seen from far away, T looks like some deterministic norm. In this talk I will try to

explain can we go further and give a (rough) estimate of the probability that T looks like some other metric instead.

14.30-15.00 Coffee

15.00-15.35 Victor Dubach: Scaling limits of descent-biased trees

The q -descent-biased distribution is a probability distribution on rooted labelled trees introduced recently by Paul Thévenin and Stephan Wagner. Therein, the probability mass of a given tree t is proportional to $q^{des(t)}$, where $des(t)$ is the number of descents in the tree t . In their paper, PT and SW proved that this random tree $T_n^{(q)}$ admits an explicit "one-ended" local limit at the root when q is fixed (i.e., independent of n).

A complementary question is that of the global limit (also known as scaling limit) of $T_n^{(q)}$. Our main result is a phase transition when q depends on n and is of the form $q = a/n$ for some fixed $a > 0$. In that regime, we establish a scaling limit for $T_n^{(q)}$ in the framework of dendrons: $T_n^{(q)}$ converges in distribution to a non-trivial random dendron that depends on a . When $a = 0$, we retrieve the trivial dendron limit of recursive trees. In addition, when q is fixed, we prove that $T_n^{(q)}$ admits the Brownian Continuum Random Tree as its scaling limit, in the sense of the Gromov-weak topology (which coincides with the topology of dendrons). This was famously proved by Aldous for Cayley trees (i.e., $q = 1$).

Joint work with Paul Thévenin and Stephan Wagner.

15.40-16.15 Tom Britton: Stochastic epidemic models with group structures

We consider a stochastic epidemic model in a community structured into small groups, having global as well as local contacts. Focus lies on comparing the probability, as well as the size, of a major outbreak, of the model with a situation that is closer to having only global contacts (homogeneous mixing). We move towards homogeneous mixing either by swapping some of the local contacts to global contacts, or by making the group sizes bigger. Joint work with Frank Ball and Peter Neal.

18.00 Dinner at Bröd och Vin for registered participants

Thursday

9.00-9.35 Ruoyu Wang: Local convergence and subtrees of trees

In this article, we study the asymptotic behavior of the number of subtrees and subtree density for a sequence of trees that converges in the Benjamini–Schramm sense. Benjamini–Schramm convergence, also called local (weak) convergence, describes the local behavior of a sequence of graphs. Here we show that for a sequence of Benjamini–Schramm-convergent trees, the average subtree entropy, i.e., the logarithm of the number of subtrees divided by the order, converges to a constant depending only on the limit. Furthermore, we show that if a sequence of trees locally converges to a limit that is not a two-way infinite path, then the subtree density, i.e., the probability of a uniformly random vertex being contained in a uniformly random subtree, also converges to a constant that depends only on the limit.

9.40-10.15 Josphe Hyde: Sharp asymmetric vertex Ramsey properties for random hypergraphs.

In 1992, Luczak, Rucinski and Voigt showed that for any graph H , a parameter $m_1(H)$ - called the 1-density - governs the threshold at which $G(n, p)$ inherits the vertex Ramsey property. In 2000, Freidgut and Krivelevich showed this threshold is sharp. In 1996, Kreuter showed that for any graphs H_1, \dots, H_r with $m_1(H_1) \geq \dots \geq m_1(H_r)$, a parameter dependent only on H_1 and H_2 governs the threshold at which $G(n, p)$ inherits the 'asymmetric' vertex Ramsey property. We prove that this threshold is sharp, including in the analogous hypergraph setting.

Joint work with Mael Kupperschmidt, and with Robert Hancock, Matthew Jenssen and Adva Mond.

10.20-10.40 Coffee

10.40-11.15 Stephan Wagner: Continuous parking sequences

Classical parking functions are defined by the following parking procedure: n consecutive parking spots are available on a street. There are n cars with preferred parking spots $\pi_1, \pi_2, \dots, \pi_n$. Now the i -th car that arrives parks in spot π_i if it is available, and otherwise in the first empty spot that comes afterwards. If the cars can successfully park according to this procedure, then $\pi_1, \pi_2, \dots, \pi_n$ is called a parking sequence.

We introduce the notion of continuous parking sequences as a continuous analogue of parking functions, where the lengths of the cars and the street can be arbitrary positive real numbers. The set of parking sequences is a union of polytopes whose volume is given by a surprisingly simple product formula. The proof of this formula is based on a certain convolution identity. Statistical properties of parking sequences chosen uniformly at random are discussed as well, especially concerning the first and last car in the sequence.

11.20-11.55 Lorents Landgren: Maximizing the number of connected spanning subgraphs

Starting with the set of connected multigraphs with n vertices and m edges, we define $c_j(G)$ to be the number of connected spanning subgraphs of G with exactly j edges. These numbers show up as coefficients of the reliability polynomial $R(G, p)$, which is the probability that G remains connected after each edge has been independently retained with probability p and otherwise deleted. It is therefore natural to ask if a given graph G can be modified to increase the c_j 's, and to try to identify the graphs that maximize these respective values.

General answers to these puzzles are known only for the cases where just one or two edges are removed, i.e. for j equal to $m - 1$ and $m - 2$. There is also a claimed but seriously flawed solution for $j = m - 3$. We present new solutions for the two latter cases. In particular, we show how the c_{m-3} -maximizing graphs can easily be constructed from the set of cubic graphs on $2(m - n)$ vertices that satisfy certain natural connectivity properties.

Lunch 12.00-13.15

13.15-13.50 Jacob Lundblad: The terminal Wiener index of random trees

The Wiener index, defined as the sum of all pairwise distances between vertices in a tree, is a well studied property for many common types of random trees. In 2009 the Terminal Wiener index was introduced by Gutman, Furtula and Petrović, motivated by potential applications in chemistry. To obtain the Terminal Wiener index of a rooted tree, for which few previous results exists, one considers instead the sum of pairwise distances between leaves. In this talk we show that for certain types of increasing trees, the difference between the average distance between random vertices and the average distance between leaves is small, corresponding to the behaviour of the Terminal- and regular Wiener indices.

13.55-14.30 TBA:

14.35-15.10 Altar Ciceksiz:

15.15 Coffee